

## Errata

### Items with asterisks will still be in the Second Printing

**Author website URL:** <http://cehs.unl.edu/EdPsych/RJSite/home>.

**\*P7.** “The square root of  $\sigma_E^2$  (i.e.,  $\sigma_E$ ) is referred to...” not “The square root of  $\sigma_E^2$  (i.e.,  $\sigma_E$ ) is referred to...”

**\*P28.** “A narrow interval indicates comparatively less **uncertainty** about a ...” not “A narrow interval indicates comparatively less certainty about a ...”

**\*P28.** There are two equations listed as 2.11. The second 2.11 equation should be labeled 2.12.

**\*P28.** Equation 2.13 should be  $(1-\alpha)\%CB: \hat{\theta} \pm z_{(1-\alpha/2)} \sigma_e(\hat{\theta})$



**P64.** To summarize our analyses, the nonlinear factor analysis provided support that a uni-dimensional model of the data is a reasonable **representation [ ] the data.** [of] is missing

**\*P70.** In Equation 4.6  $g(\theta | \underline{g})$  should be  $g(\theta | \underline{\nu})$

**\*P73.** Equation 4.7 should be  $\frac{\partial}{\partial \delta_j} \ln L = - \sum_r^R \sum_i^N \{ [x_{ij} - p_j(X_r)] [p_j(X_r | \underline{x}_i, \underline{g}, \underline{\nu})] \} = 0$  .

Equation 4.9 should be

$$\frac{\partial}{\partial \delta_j} \ln L = - \sum_r^R \sum_i^N \{ [x_{ij} * p_j(X_r | \underline{x}_i, \underline{g}, \underline{\nu})] - [p_j(X_r) * p_j(X_r | \underline{x}_i, \underline{g}, \underline{\nu})] \} = 0 .$$

Equation 4.10 should be

$$\frac{\partial}{\partial \delta_j} \ln L = - \sum_r^R \left\{ \left[ \sum_i^N x_{ij} * p_j(X_r | \underline{x}_i, \underline{g}, \underline{\nu}) \right] - \left[ p_j(X_r) \sum_i^N p_j(X_r | \underline{x}_i, \underline{g}, \underline{\nu}) \right] \right\} = 0 .$$

Equation 4.11.  $p \rightarrow p_j$  &  $\bar{n}_{ij} = \sum_i^N p_j(X_r | \underline{x}_i, \underline{g}, \underline{\nu})$

**P79.** Table 4.1.  $PSD(\hat{\theta}) = \frac{0.0624150}{0.1174369} = 0.7290 \rightarrow PSD(\hat{\theta}) = \sqrt{\frac{0.0624150}{0.1174369}} = 0.7290$

**\*P86.** Line 1: Should read:  $A(X_1) = 0.7648E-04 = 0.00007648$

**\*P86.** Line 17: “ $\alpha_j \sqrt{1 + \alpha_j^2}$ ” should be  $\alpha_j / \sqrt{1 + \alpha_j^2}$

**\*P90.** Line 6: `IFNAME='C:\MATHRSCH.dat'` should be `IFNAME='C:\MATHRSCH.PAR'`

**P92.** (just below Equation 4.17).  $\xi^*$  is the  $\delta_j^*$  (or  $\theta$ ) is the  $\delta_j$  on the target metric  $\rightarrow \xi^*$  is the  $\delta_j^*$  (or  $\theta^*$ ) is the target metric.

**\*P93.** Equation 4.21 should read  $\kappa = \bar{\delta}^* - \zeta \bar{\delta}$

**P100.** (just above Figure 5.1).  $p(x=1|\theta, \alpha_j, \delta_j) \rightarrow p(x_j=1|\theta, \alpha_j, \delta_j)$

**\*P120.** Equation 5.15.  $p_j' = \alpha_j \frac{e^{\alpha_j(\theta-\delta_j)}}{(1+e^{\alpha_j(\theta-\delta_j)})(1+e^{\alpha_j(\theta-\delta_j)})} = \alpha_j \frac{e^{\alpha_j(\theta-\delta_j)}}{[1+e^{\alpha_j(\theta-\delta_j)}]^2}$

**P141.**  $R_\Delta^2 = \frac{110774.295 - 110397.103}{110774.295} = 0.003 \rightarrow R_\Delta^2 = \frac{110397.103 - 110064.929}{110397.103} = 0.003$

**P143.** Equation 6.8. There is no closing parenthesis or the opening parenthesis may need to be removed.

**P160.** The last line. Equation 6.21  $\rightarrow$  Equation 6.22

**\*P160.** Equation 6.22 should read:  $w_j(\theta) = \frac{\alpha_j(p_j - \chi_j)}{p_j(1 - \chi_j)} = \frac{\alpha_j}{1 + \chi_j e^{-\alpha_j(\theta - \delta_j)}}$

**P165.**  $\frac{e^{(\theta - \delta_2)}}{\theta} \rightarrow \frac{e^{(\theta - \delta_2)}}{\varphi}$

**\*P165.** Second paragraph, last sentence should read “The probability of both of these is given by adding the (mutually exclusive) events of 0 and 1, that is,  $e^{0+(\theta - \delta_1)}$  .

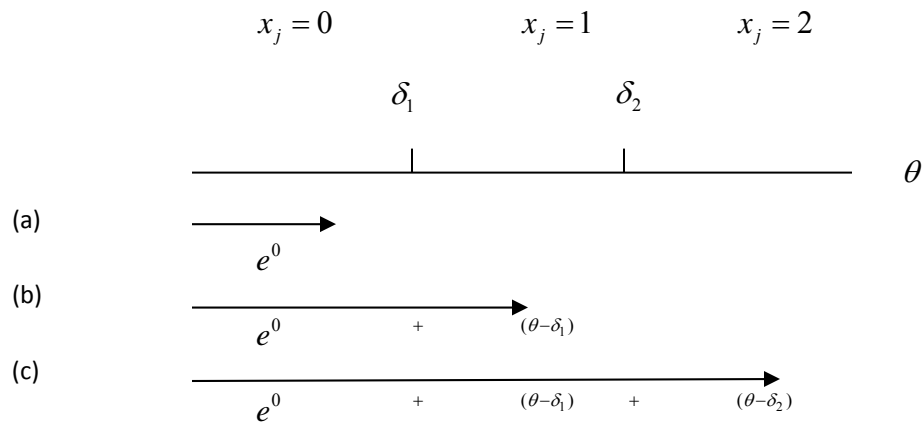
**\*P165.** Third paragraph, fourth and fifth sentences should read “Therefore, to obtain an  $x_j = 2$  the individual passes through  $x_j = 0$  (i.e.,  $e^0$ ), passes through  $x_j = 1$  (i.e.,  $e^{0+(\theta-\delta_1)}$ ), *and* then passes through the second transition point (i.e.,  $e^{0+(\theta-\delta_1)+(\theta-\delta_2)}$ ). Therefore, the probability of  $x_j = 2$  is given by  $e^{0+(\theta-\delta_1)+(\theta-\delta_2)}$ .

**\*P165.** Fourth paragraph, first sentence should read “When each of the three terms (i.e.,  $x_j = 0$ :  $e^0$ ,  $x_j = 1$ :  $e^{0+(\theta-\delta_1)}$ ,  $x_j = 2$ :  $e^{0+(\theta-\delta_1)+(\theta-\delta_2)}$ ) is ...”

**\*P165.** Figure 7.1:

panel a:  $e^0$                                   panel b:  $e^{0+(\theta-\delta_1)}$                                   panel c:  $e^{0+(\theta-\delta_1)+(\theta-\delta_2)}$

Therefore, Figure 7.1 should appear as:



**\*P171.** Table 7.1 'NEXAMINEES=3000' should be 'NEXAMINEES=2942'

**\*P180.** “For example, let  $\tau_1$ ,  $\tau_2$ ,  $\tau_3$  have the values of -0.8, -0.2, and 0.5, respectively, and let ...” should be “For example, let  $\tau_1$ ,  $\tau_2$ ,  $\tau_3$  have the values of -0.8, -0.2, and 1.0, respectively, and let ...”

**P177.** The last paragraph. There is no A, B, and C in Figure 7.7. Figure 7.7A, Figure 7.7B, and Figure 7.7C correspond to the top, middle, and bottom graphs, respectively.

**P197.** 12<sup>th</sup> line from the bottom. 1.3 logit  $\rightarrow$  2.1 logit ( $-90 - 1.26 = -2.16$ ). 4<sup>th</sup> line from the bottom. “strongly agree”  $\rightarrow$  “strongly disagree”

**P199.** 19<sup>th</sup> line from the top. 22 respondents.  $\rightarrow$  45 respondents (180 people/4 categories=45)

**\*P210.** First full paragraph, first sentence: "... an item  $\delta_{jk}$  s ..." should be "... an item  $\delta_{jh}$  s ..." and in the last sentence of this paragraph "... substituting  $\delta_{jk} = \delta_j - \tau_k$  ..." should be "... substituting  $\delta_{jh} = \delta_j - \tau_h$  ..."

**P212.** Figure 8.2  $\alpha$  s should be  $\alpha_2$ .

**P225.** 14<sup>th</sup> line from the top. the approximate range of -1.57 to 1.23  $\rightarrow$  the approximate range of -1.88 to 1.23 (item 6's  $\hat{\delta}_{j1} = -1.88$ )

**\*P231.** Equation 8.8 should be: 
$$I_{x_j}(\theta) = \frac{\{p_{x_j}\}^2}{P_{x_j}} = \frac{[P_{x_j}^{*1} - P_{x_{j+1}}^{*1}]^2}{P_{x_j}^{*1} - P_{x_{j+1}}^{*1}}$$

**\*P231.** The first equation after "so that" in the bottom half of this page should be:

$$p'_0 = [P_0^{*1} - P_1^{*1}] = 0 - \alpha_j \left( \frac{e^{\alpha_j(\theta - \delta_1)}}{\varphi_1} \right) = -\alpha_j \left( \frac{e^{\alpha_j(\theta - \delta_1)}}{\varphi_1} \right)$$

**\*P232.** The first equation should be:

$$\begin{aligned} p'_1 = [P_1^{*1} - P_2^{*1}] &= \alpha_j \left( \frac{e^{\alpha_j(\theta - \delta_1)}}{\varphi_1} \right) - \alpha_j \left( \frac{e^{\alpha_j(\theta - \delta_2)}}{\varphi_2} \right) \\ &= \alpha_j \left[ \left( \frac{e^{\alpha_j(\theta - \delta_1)}}{\varphi_1} \right) - \left( \frac{e^{\alpha_j(\theta - \delta_2)}}{\varphi_2} \right) \right] \end{aligned}$$

**P234.** Equation 8.10.  $x_k \rightarrow x_{jk}$

**P250.** The clause after the semicolon should read:

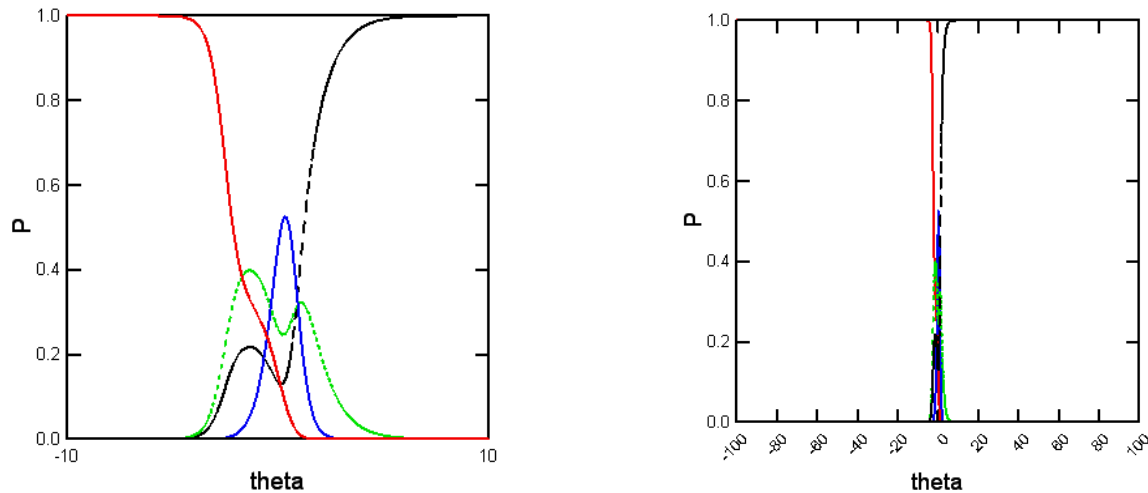
" in this case the corresponding HIGH category identification does not need to be changed (i.e., HIGH=(2,3,4,3))."

**\*P251.** Last line of the paragraph that continues from p. 250: "...; we use the  $2\ln L$  value below." should read "...; we use the  $-2\ln L$  value below."

**\*P266.** First full paragraph, line 5: “.. the difference chi-square is  $288.4 - 259.73 = 29.1$ ” should read “.. the difference chi-square is  $288.4 - 259.3 = 29.1$ ”

**\*P266.** Second to last sentence in the first full paragraph: “With a critical  $X^2$  of ...” should be “With a critical  $X^2$  of ...” (i.e., chi square is not italicized)

**\*P268.** Item 4’s ORFs for the theta range -10 to 10 (left panel) and -100 to 100 (right panel)



**P279.** 9<sup>th</sup> line from the bottom. According to Figure 10.3, the rightmost line is related to  $p_j = 0.95$  instead of  $p_j = 0.90$

$$\mathbf{P294.} \quad \gamma_j^* = \gamma_j \frac{\alpha_j(\kappa)}{\zeta} \rightarrow \gamma_j^* = \gamma_j - \frac{\alpha_j(\kappa)}{\zeta}$$

**\*P296.** Table 10.1’s Note should read “Name=intrprsnl.inp”

**\*P313.** Equation 11.6 should read  $\kappa = \bar{\delta}^* - \zeta \bar{\delta}$

**\*P320.** Table 11.3: The initial value of the K should be 0.20 not 0.10. Therefore,

INITIAL VALUE FOR A= 0.8000 INITIAL VALUE FOR K= 0.1000

should be

INITIAL VALUE FOR A= 0.8000 INITIAL VALUE FOR K= 0.2000

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**\*P331.** The TSW  $\Delta G^2$  DIF approach can be performed using either MULTILOG or IRTLRDIF (Thissen, D. (2001). *IRTLRDIF v2.0b: Software for the computation of the statistics involved in item response theory likelihood-ratio tests for differential item functioning* [Computer software and manual]. Chapel Hill: L.L. Thurstone Psychometric Laboratory, University of North Carolina.)

**\*P338.** The  $\Delta G^2$  should read 41.407 not 44.407.

**\*P338.** The estimated full model should be:

$$z_3 = -1.3330 + 0.1371 * X + 0.7714 * RACE - 0.1171(X * RACE)$$

**\*P338.** The estimated reduced model (1) should be:

$$z_3 = 0.5558 + 0.0481 * X - 1.9577 * RACE$$

**\*P339.** Table 12.4 should read:

```
/* Full Model */
```

```
The LOGISTIC Procedure
```

```
:
```

```
Model Fit Statistics
```

Criterion	Intercept Only	Intercept and Covariates
AIC	2568.331	2225.517
SC	2573.947	2247.980
-2 Log L	2566.331	2217.517

```
Testing Global Null Hypothesis: BETA=0
```

Test	Chi-Square	DF	Pr > ChiSq
Likelihood Ratio	348.8144	3	<.0001
Score	302.5715	3	<.0001
Wald	238.7854	3	<.0001

```
The LOGISTIC Procedure
```

```
Analysis of Maximum Likelihood Estimates
```

Parameter	DF	Estimate	Standard Error	Wald Chi-Square	Pr > ChiSq
Intercept	1	-1.3330	0.3626	13.5133	0.0002
X	1	0.1371	0.00860	5.3560	0.0207
RACE	1	0.7714	0.4484	2.9596	0.0854
X*RACE	1	-0.1171	0.0193	36.9106	<.0001

```
:
```

```
/* reduce model (1)/"full" model */
```

```
Last updated 4/14/20
```

:

```

                                Model Fit Statistics
                                Intercept
                                and
                                Covariates
Criterion      Intercept Only      2264.923
AIC            2568.331            2264.923
SC             2573.947            2281.771
-2 Log L      2566.331            2258.923

Testing Global Null Hypothesis: BETA=0
Test           Chi-Square      DF      Pr > ChiSq
Likelihood Ratio      307.4075      2      <.0001
Score               292.7168      2      <.0001
Wald                262.7802      2      <.0001

Analysis of Maximum Likelihood Estimates
Parameter      DF      Estimate      Standard      Wald      Pr > ChiSq
Intercept      1      0.5558      0.1880      8.7427      0.0031
X              1      0.0481      0.00749     41.2621     <.0001
RACE           1      -1.9577     0.1211     261.3266     <.0001

Odds Ratio Estimates
Effect         Point      95% Wald
              Estimate      Confidence Limits
X              1.049     1.034      1.065
RACE           0.141     0.111     0.179

```

**\*P340.** The second to the last sentence in the paragraph should read: “Given our coding of the RACE variable if  $\hat{\tau}_2 < 0$ , then the item favors the focal group. In contrast, if  $\hat{\tau}_2 > 0$  then the item favors the reference group.”<sup>6</sup>

**\*P340.** Table 12.5 should read:

```
/* reduce model (2) */
```

:

```

                                Model Fit Statistics
                                Intercept
                                and
                                Covariates
Criterion      Intercept Only      2569.709
AIC            2568.331            2569.709
SC             2573.947            2580.941
-2 Log L      2566.331            2565.709

Testing Global Null Hypothesis: BETA=0
Test           Chi-Square      DF      Pr > ChiSq
Likelihood Ratio      0.6217      1      0.4304
Score               0.6223      1      0.4302
Wald                0.6221      1      0.4303

Analysis of Maximum Likelihood Estimates
Parameter      DF      Estimate      Standard      Wald
Intercept      1      0.5558      0.1880      8.7427
X              1      0.0481      0.00749     41.2621
RACE           1      -1.9577     0.1211     261.3266

```

Last updated 4/14/20

Parameter	DF	Estimate	Error	Chi-Square	Pr > ChiSq
Intercept	1	0.8521	0.1727	24.3530	<.0001
X	1	-0.00488	0.00619	0.6221	0.4303

Effect	Odds Ratio Estimates		
	Point Estimate	95% Wald Confidence Limits	
X	0.995	0.983 1.007	

**\*P345.** Endnote 6. Reduced model (1): should be

$$z_3 = 0.5558 + 0.0481 * X - 1.9577 * RACE$$

and the corresponding text should read:

“Therefore, holding the observed score fixed and switching from the focal group to the reference group results in a decrease in the log odds of obtaining a response of 1 by 1.9577. In terms of odds we have that the odds that a reference group member will produce a response of 1 are  $\exp(-1.9577) = 0.1412$  to 1 (note: 0.141 is the value listed as the Point Estimate in the Odds Ratio Estimates section). Alternatively, holding the observed score fixed, one expects the odds of focal group members to correctly respond to the item to be roughly 7 to 1 (i.e.,  $1/0.1412 = 7.0830$ ) relative to comparable reference group members.”

**P356.** 16<sup>th</sup> line from the top. if  $q_j = 0$ , then  $\delta = \infty$ , and if  $q_j = N$ , then  $\delta = -\infty$

**P357. First Equation:** negative sign in from of  $q_j$ :

$$\frac{\partial}{\partial \delta} \ln L(\underline{x} | \delta'_j) = -q_j + \sum_{i=1}^N p_{ij}^{(t)}$$

**P358. B.4's** subscripts are not formatted properly. It should appear as:

$$\sigma_e(\hat{\delta}) = \frac{1}{\sqrt{\sum_{x=1}^{L-1} n_x p_{xj} * (1 - p_{xj})}}$$

**P372.** The last equation should be labeled C.34. The paragraph should read:

If we take our total sample of individuals and divide it into subgroups and we redefine the standard deviation in Equation C.33 to be the standard deviation of a subgroup,  $\sigma_i$ , with mean  $\mu_i$ , then its substitution into Equation C.2 gives Thurstone's mental age model; we're assuming that each subgroup is normally distributed. That is, Thurstone (1925; e.g., see p. 441) developed a



model based on the cumulative normal distribution to determine the proportion of individuals of a specified age group correctly responding to an item.

**P405.** Equation E.24.  $\chi_{sc}^2 \rightarrow \chi_{sc}^2 =$

**P406.**  $\kappa = \bar{\delta}^* - \zeta(\bar{\delta}) = 51.3 - 1.80(10.7) = 32$

**P407.**  $\kappa = \bar{\delta}^* - \zeta(\bar{\delta}) = 81.5 - 1.80(27.5) = 32$